

Case History	Vibration of Ball Pass Frequency Occurred in Multi-Disk Spindle System	Information equipment
Resonance		

Object Machine	Large-scale hard disk assembly (HDA, Fig. 1)	
Observed Phenomena	At the rated rotational speed of 60 rps=3,600 rpm, abnormal vibration (the predominant frequency is 380 Hz and amplitude about 0.8 $\mu\text{m}$ ) appeared in the position signal that represents relative gap between the rotating disk and the stationary magnetic head, as shown in Fig.2. This excessive vibration induced error signal by the defectiveness of head positioning function.	
Cause Presumed	From evaluating the fact that vibration was observed even when the head was not accessed, and that the vibration frequency coincided with some relations to the ball pass frequencies of ball bearings. The vibration is predicted by being caused in the spindle system.	
Analysis and Data Processing	<p>In order to clarify the rotational vibration characteristic of the spindle, the harmonic wave excitation force was applied to the HDA device using a shaking apparatus shown in Fig.3. In addition, variable speed operation was performed to measure radial vibrations of the shaft and hub using a non-contact displacement pick-up. The shaft FRA (frequency response analysis) curves are shown in Fig. 4 and the hub FRA curves are seen in Fig.5 (upper two curves). The base FRA (acceleration) and the excitation force are also included in Fig.5. The position signal response is shown in Fig.6. Figure 7 indicates the vibration mode of the shaft and the hub.</p> <p>As summarized in Fig.8, all of frequencies of resonance peaks of FRA curves are plotted for each rotational speed at which the excitation was done. From these data mentioned above, we clarified that the 380 Hz vibration is of a shaft tilting mode including the base structural deformation and resonated with an excitation frequency + 6.42 <math>\Omega</math> caused by inner ring swell of ball bearing (refer to Table 1).</p> <p>Meanwhile, a detailed modeling and the corresponding vibration calculation were conducted using the 3D FEM for the disk spindle system and using 1D-FEM (beam element only) for analyzing the natural frequency and shaft resonant modes. Figure 9 shows the analysis model and calculation results. According to these calculation results, it is known that the 4th mode corresponds to the resonant frequency of 380 Hz, which is in good agreement with experimental results.</p>	
Countermeasures and Results	Based on the above discussion, countermeasures were taken to enhance the bending stiffness of the bearing housing standing the base. Prior to manufacture of the parts for the countermeasures, the calculated eigenvalues of the rotor system were checked and examination was made to avoid the resonance of 380 Hz at the rated speed 60 rps. Moreover, accuracy of single ball bearing unit to be assembled was improved, thus restraining abnormal vibration.	
Lesson Learned	In the case of super-precision machine like HDA, little deformation of ball bearings generates an inherent excitation force. It is thus important to design the avoidance of the resonance due to ball pass frequencies in relation to the rotor system and the base system.	
References	Matsushita, et al. "Ball Pass Frequency Analysis of Magnetic Disk Spindle System", <i>Transactions of the JSME</i> (Edition C), Vol 52, Series 474 (1986: 439-447)	
Keyword	Rotating machinery, vibration of rotating body, rotating circular plate, ball bearing, vibration mode, vibration analysis, vibration measurement, ball pass frequencies, resonance vibration	

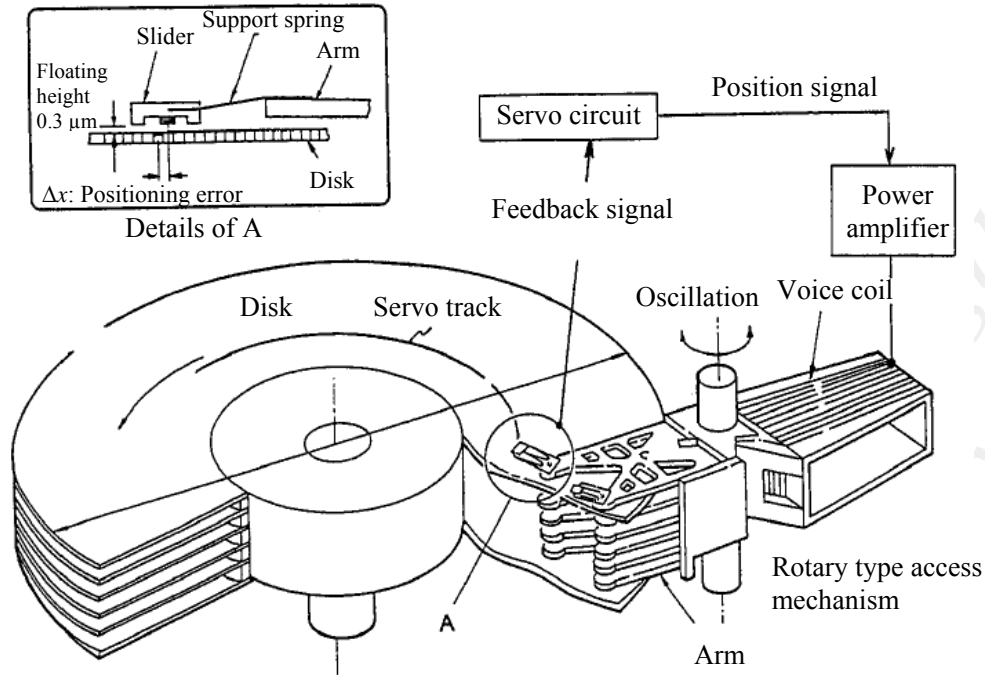


Fig.1: Conceptual drawing of position signal

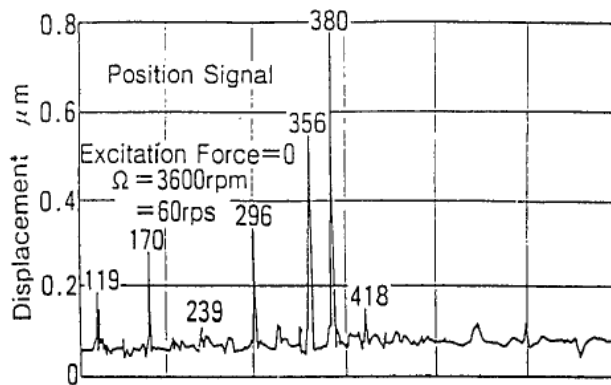


Fig.2: Amplitude of position signal

#### Equipment specification

Disk outer diameter $\times$ plate thickness $\times$ number of sheets:	14 inch $\times$ 1.9 $\times$ 13 ( $\phi$ 357)
Memory capacity/spindle:	600 MB
Rated rotational speed:	3,600 rpm
Head access type:	rotary ( $\times$ 2)
Equipment weight/spindle:	about 60 kg
Support bearing:	single row deep groove ball bearing (6207, 6206)

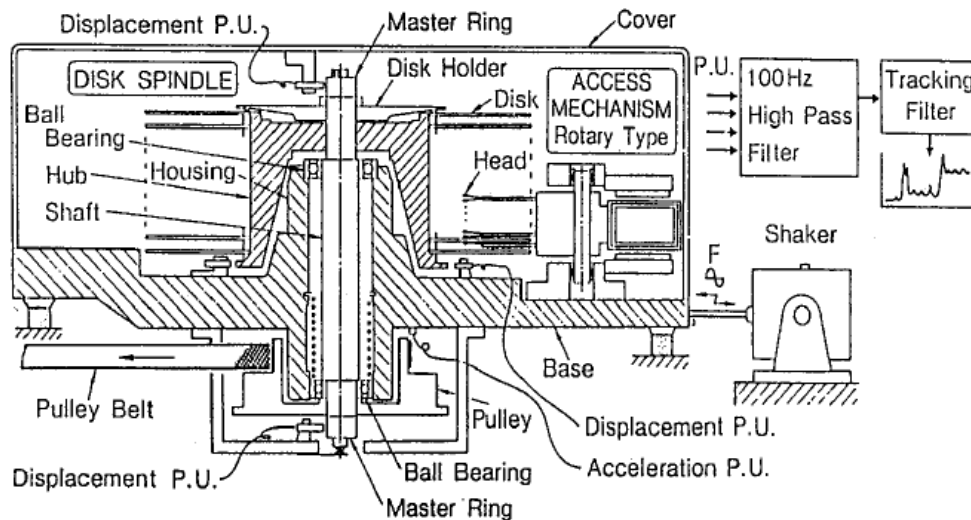


Fig.3: Experimental excitation apparatus

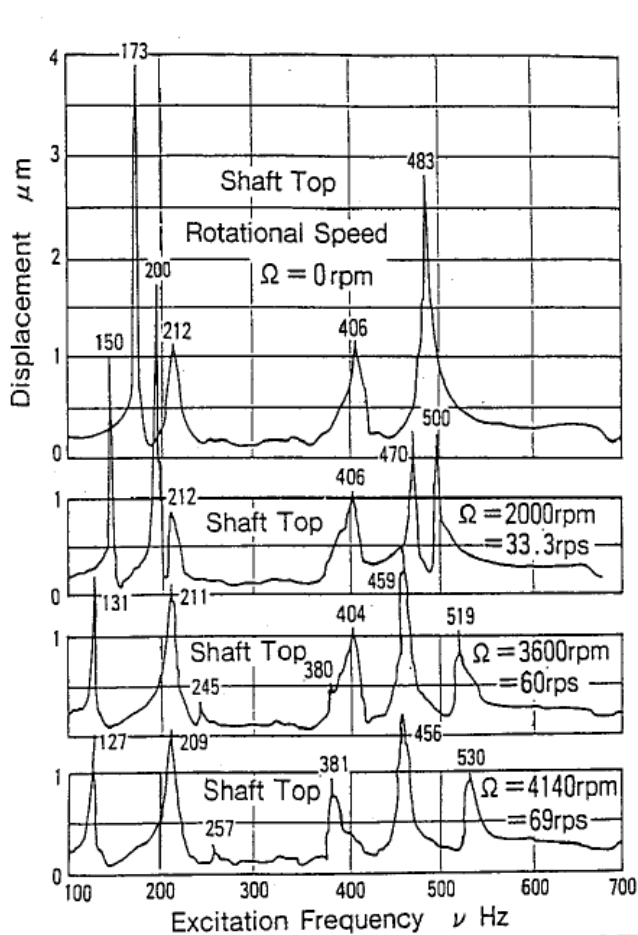


Fig.4: Response curves for sinusoidal excitation (main axis top)

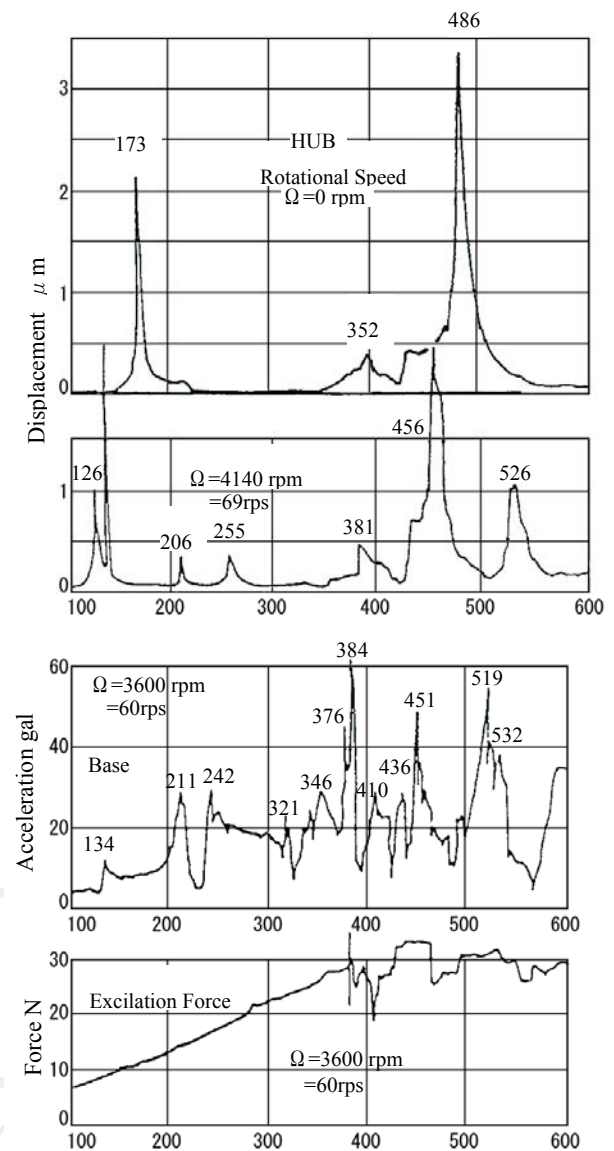


Fig.5: Response curves for sinusoidal excitation

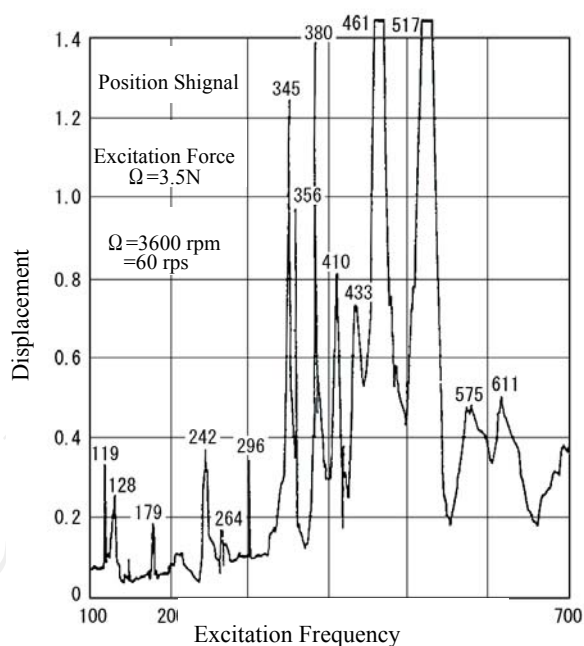


Fig.6: Response curves for sinusoidal excitation (position signal)

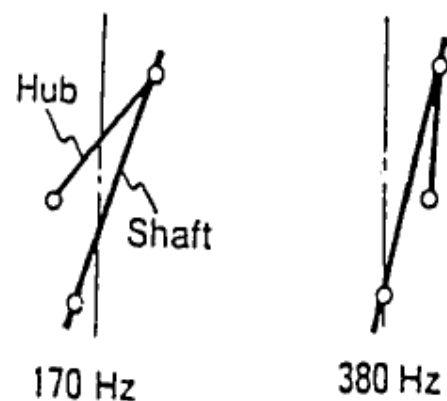


Fig.7: Results of experiment (vibration mode)

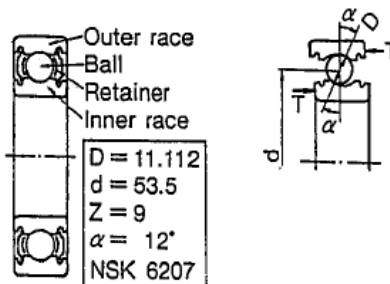
Deformation	Excitation Frequency
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Bearing Race	Number	Forward	Backward
INNER	1	$(Z+1-Z\beta)\Omega$	$-(Z-1-Z\beta)\Omega$
	m	$(mZ+1-mZ\beta)\Omega$	$-(mZ-1-mZ\beta)\Omega$
OUTER	1	$+Z\beta\Omega$	$-Z\beta\Omega$
	m	$-mZ\beta\Omega$	$-mZ\beta\Omega$





$\Omega_r$  : rotating retainer frequency  
relative to the stationary  
outer race

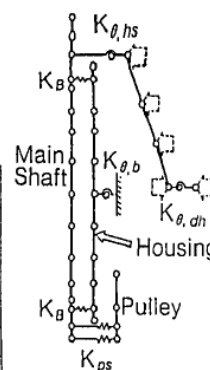
Outer race  
Ball  
Retainer  
Inner race

$D = 11.112$   
 $d = 53.5$   
 $Z = 9$   
 $\alpha = 12^\circ$   
 NSK 6207



$K_{\theta,hs} = 5.9 \times 10^8 \text{ N.mm/rad}$
$K_{ps} = 5.9 \times 10^3 \text{ N./mm}$
$K_{\theta,dh} = 4.2 \times 10^6 \text{ N.mm/rad}$
$K_{\theta,b} = 2.0 \times 10^9 \text{ N.mm/rad}$

Eigen Mode Shape				
EXP.	—	160Hz	216Hz	368Hz
CAL.	72Hz	170Hz	212Hz	378Hz



standstill)